

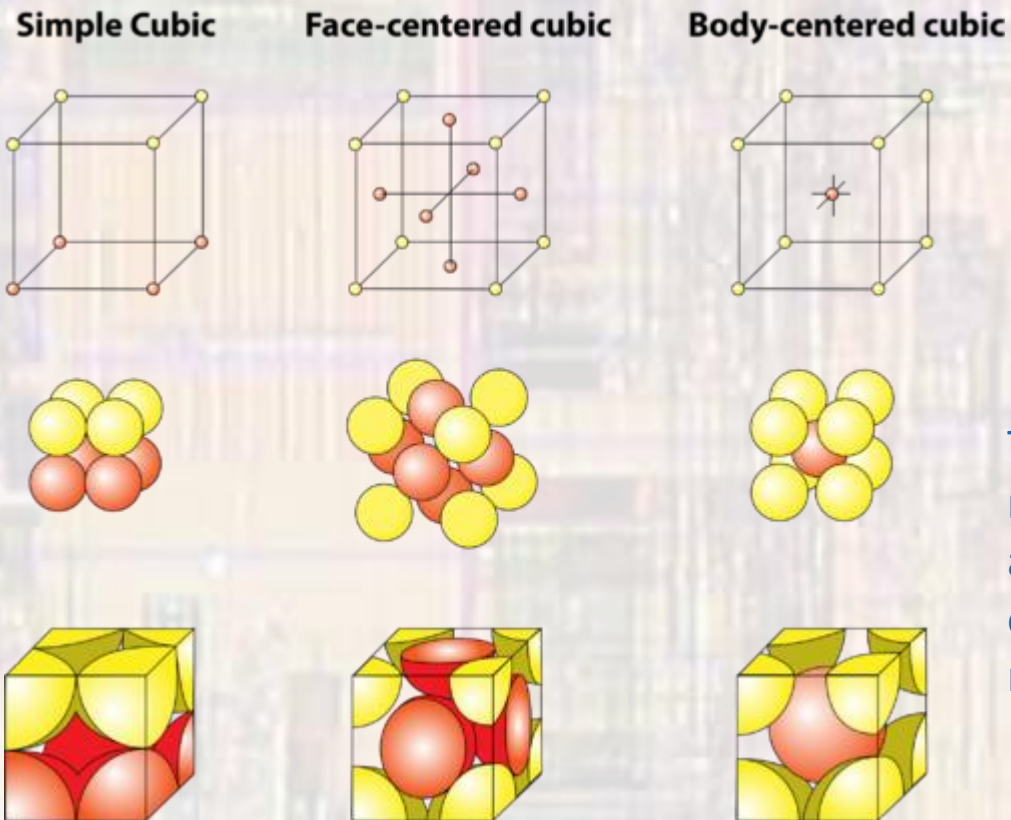
# Silicon Crystal Structure

Last updated 2/26/22

These concepts have been greatly simplified

# Silicon Crystal Structure

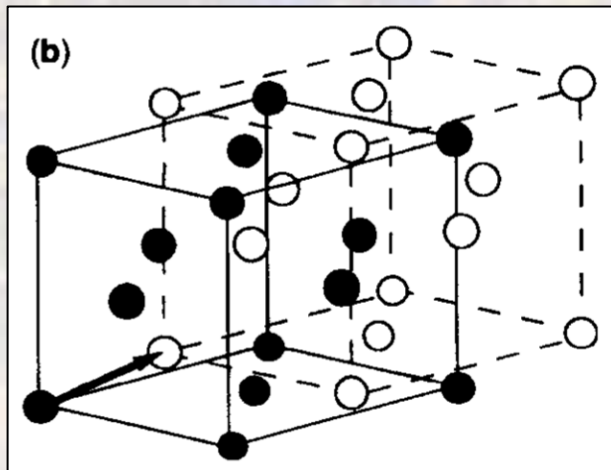
- Crystals are characterized with 3d geometric structures (unit cell)



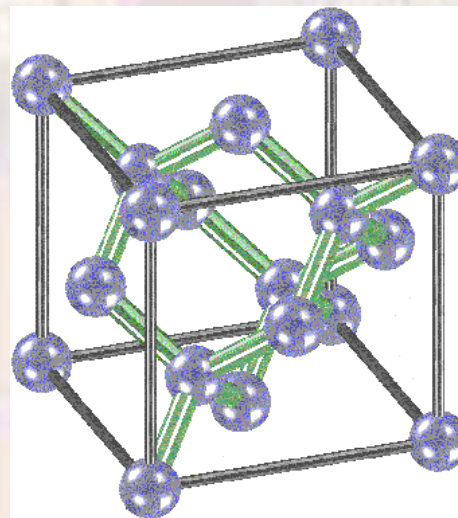
The spheres here represent the approximate extents of the atom, not the nuclei

# Silicon Crystal Structure

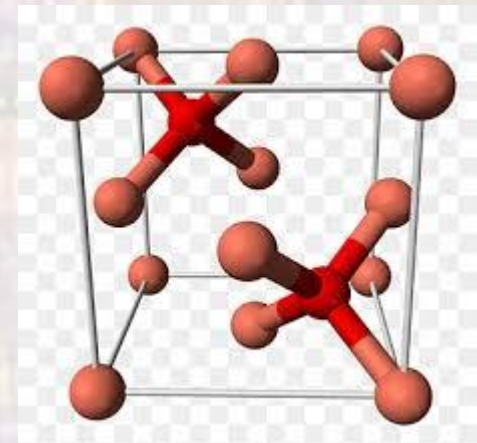
- Silicon unit cell
  - 2 interpenetrating Face Centered Cubic Cells



2 FCC cells  
1 shifted  $\frac{1}{4}$  of the way  
along the major diagonal



Resulting diamond  
cubic lattice



Atoms showing  
4 nearest neighbor  
structure

Lattice parameter (edge length) of 0.543 nm  
Nearest neighbor distance is 0.235 nm.

# Silicon Crystal Structure

- Silicon unit cell
    - Corners: 8, 1/8 atoms/unit cell      1
    - Faces: 6, 1/2 atoms/unit cell      3
    - Inside: 4 full atoms/unit cell      4
- 8 atoms/unit cell

Cell volume:

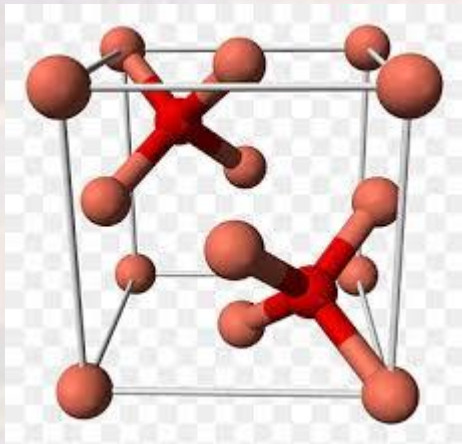
$$(.543 \text{ nm})^3 = 1.6 \times 10^{-22} \text{ cm}^3$$

Density of silicon atoms

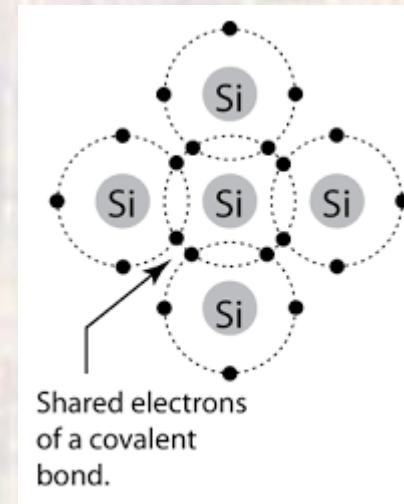
$$= (8 \text{ atoms}) / (\text{cell volume}) = 5 \times 10^{22} \text{ atoms/cm}^3$$

# Silicon Crystal Structure

- Silicon unit cell – bonding model
  - Si has a half full outer electron shell (4 / 8)
  - Lowest energy state is the Diamond Lattice
    - 4 electrons are shared between 4 nearest neighbors



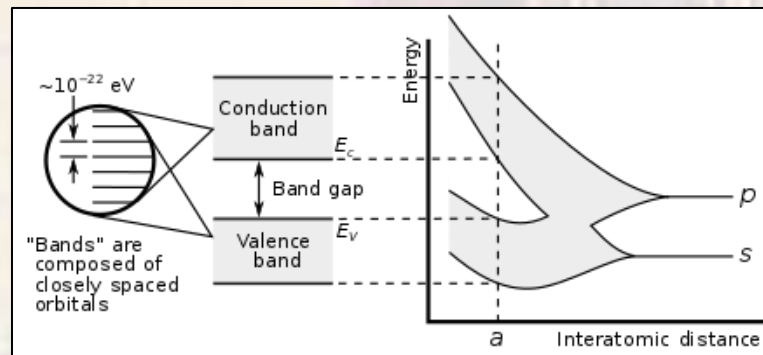
Atoms showing  
4 nearest neighbor  
structure



Each atom appears to have a full  
valence band → very stable

# Silicon Crystal Structure

- Silicon Crystal – binding energies
  - The net effect of combining into the crystal structure is that the allowed energy states are modified
    - A group of allowed **low** energy states is formed
      - Valence Band
      - At 0K, all of the electrons are in these bands
    - A group of allowed **high** energy states is formed
      - Conduction Band
      - At 0K, no electrons are in these bands
    - A gap, where no allowed energy states exist is created
      - Bandgap



4 allowed states / atom  
in each band

# Silicon Crystal Structure

- Silicon Crystal – binding energies
  - As temperature is increased – some electrons acquire enough energy to “jump” the bandgap and move from a valence band state to a conduction band state
  - These electrons can move freely through the crystal while in the conduction band
  - Once an electron has left the valence band, there is a missing bond (electron) in the structure (Hole)
  - These holes can move freely through the crystal while in the valence band

# Silicon Crystal Structure

- Intrinsic carrier density
  - How many electrons have moved from the valence band to the conduction band

$$n_i = BT^{3/2} e^{\frac{-E_g}{2kT}}$$

B – semiconductor specific coefficient

T – temperature in Kelvin

$E_g$  – semiconductor band gap energy in eV

k – Boltzmann's constant ( $86 \times 10^{-6}$  eV/K)

For Si:

$$B = 5.23 \times 10^{15} \text{ cm}^{-3} \text{ K}^{-3/2}$$

$$E_g = 1.2 \text{ eV (0K)}, 1.1 \text{ eV (300K)}$$

at 300K (room temp?)  $\rightarrow n_i = 1.5 \times 10^{10} / \text{cm}^3$



# Silicon Crystal Structure

- Intrinsic carrier density

$$5 \times 10^{22} \text{ atoms/cm}^3$$

$$1.5 \times 10^{10} \text{ electrons/cm}^3$$

one in  $3.3 \times 10^{12}$  electrons has been elevated  
1 in 3 Trillion

$$\text{resistivity } \rho = 3.4 \times 10^5 \Omega\text{-cm}$$