

No note-sheets, calculators, or other study aids on this exam. Write your initials at the top of each page except this one. Read through the whole exam before you get started.

Have fun!

- (2 points) **Select one:** To ensure print jobs are handled in the order they are received, they should be stored in...
 - A LinkedList
 - A Queue
 - A Stack
 - An ArrayList
- (2 points) **Select one:** If a queue is implemented by wrapping Java's LinkedList, and the poll method is implemented with `list.remove(0)`, the offer method should be implemented with
 - `list.get()`
 - `list.get(list.length()-1)`
 - `list.add(e)`
 - `list.add(list.length()-1,e)`
- (2 points) **Select one:** A stack is:
 - MIMO
 - LIFO
 - FIMO
 - FIFO
- (2 points) Suppose a queue is implemented by wrapping Java's ArrayList, with the front of the queue at index 0 and the back (rear) of the queue at index $n-1$. **Write** the Big-O runtime for the following methods:
 - `queue.poll()`
 - `queue.offer(E e)`
 - `queue.peek()`
 - `queue.isEmpty()`
- (4 points) **Describe** an error that our Stack interface can help you catch at compile-time.
- (5 points) **Describe** the difference between the `offer(e)` and `add(e)` methods of Java's Queue interface.
- (3 points) **Give an example** of when you would want to use Java's `add(e)` instead of `offer(e)`, and when you would want to use Java's `offer(e)` instead of `add(e)`.
- (5 points) The items 8 5 7 2 1 4 are put onto a queue in that order. **Write** the items in the order they will come off the queue.

9. Consider the circular queue we implemented in class:

```
public class CircularQueue<E> implements Queue<E> {
    private final int MAX_SIZE = 6; // max number of elements that can be held
    private int indFront = 0; // index of "front of the line", or 0 if empty
    private int indRear = -1; // index of "back of the line", or 0 if empty
    private E[] array = (E[]) new Object[MAX_SIZE];
    //... methods will go here...
}
```

- a. (5 points) Implement an isEmpty method that returns true if the queue is currently empty

- b. (5 points) Write a helper method willBeEmpty that is true if (and only if) removing another item from the queue will make the queue empty.


```
private boolean willBeEmpty() {
    }

```
- c. (10 points) **Draw** the contents of array after offering 1 5 3 6 2 to a CircularQueue<Integer> in that order, calling poll twice, then offering 8 9 4. Your diagram should make clear what the index and contents of each element of the queue are. **Show** your work.

- d. (5 points) **Write** whether the CircularQueue behaves any differently from a LinkedList from the client code's perspective. **Explain** your answer.

10. (10 points) Consider the expression represented by the recursive sequence

$$a_n = a_{n-1} + 5 \quad n > 1$$

$$a_1 = -4$$

Write a recursive method to compute $a(n)$

11. a. (5 points) **Determine** how many times the recursive method below will be called while evaluating $m(2)$, include the first call. (Note: This is not the most efficient recursive implementation.) **Show** your work.

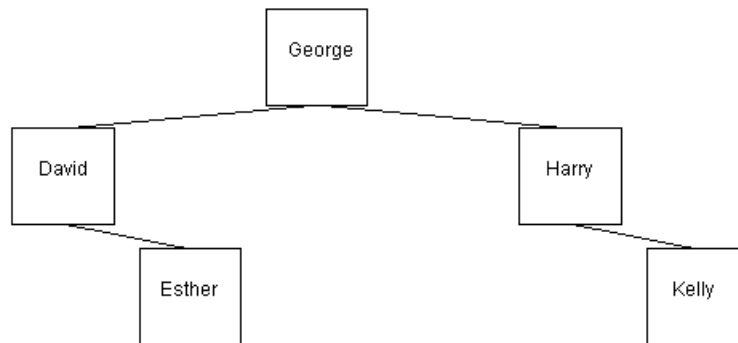
```
public int m(int x) {  
    if (x <= 1) {  
        return 1;  
    } else {  
        return m(x-1)-m(x-2);  
    }  
}
```

b. (5 points) **Determine** what the return value of $m(2)$ will be. **Show** your work.

12. (5 points) Consider a binary search of an array. With n comparisons (for some n that you don't need to know), you can search 16,383 elements. **Determine** how many elements you can search with $n+1$ comparisons. **Show** your work.

13. (5 points) A Binary Search Tree and a Linked List have a similar structure. **Explain** the advantage of a Binary Search Tree's structure.

14. (10 points) **Insert** Alice, Fred, Joe, and Mike into this Binary Search Tree without changing any non-null references.



15. (10 points) **Implement** the `size()` method of a Binary Search Tree, like the one we defined in class. If you call any other methods of this class, write the method as part of your solution.

```
public class BinarySearchTree<E extends Comparable<E>> {  
    private Node root;  
    private class Node {  
        private Node left;  
        private Node right;  
        private E value;  
        private Node(Node left, Node right, E value) { /* ... */ }  
    }  
}
```

}